

## Solutions for Assignment #11

### Assignment Information

Maximum grade 20

Due date December 8, 2004

Instructions Textbook:  
Page: 214  
Problems: 5.4.3, 5.4.5

5.4.3

$S \rightarrow aS \mid aTbS \mid \epsilon$

$T \rightarrow aTbT \mid \epsilon$

5.4.5 a) Show that this grammar is unambiguous.

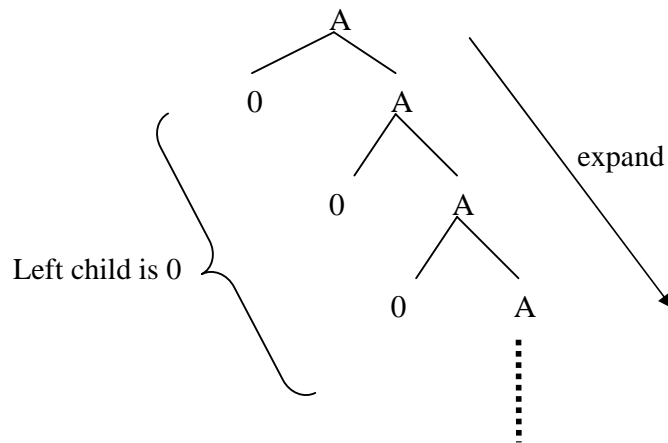
This grammar is unambiguous because of following reasons.

$S \rightarrow A1B$

S is replaced by A1B. "1" is between A and B, so "1" divides S into A and B. S has only one production.

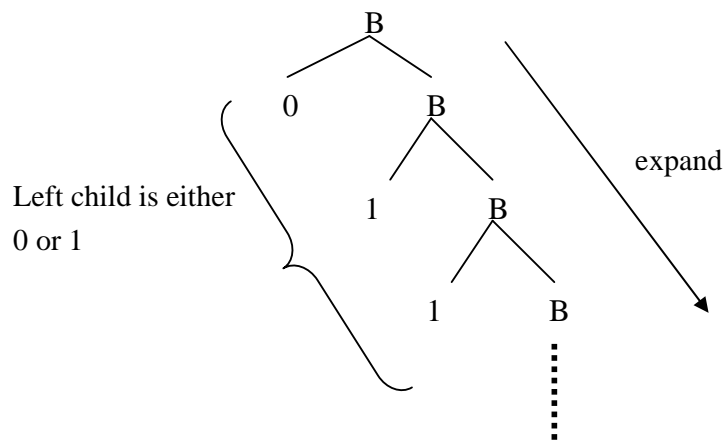
$A \rightarrow 0A \mid \epsilon$

A is replaced by 0A or  $\epsilon$ . " $A \rightarrow 0A$ "  $\mid \epsilon$ " does not make this grammar ambiguous. (= unambiguous) As shown following tree, this  $A \rightarrow 0A$  replaces A to 0A. The structure of this tree is unique and expands to the right side. Left child must have 0 and right child must have A or  $\epsilon$



$B \rightarrow 0B \mid 1B \mid \epsilon$

B is replaced by 0B, 1B or  $\epsilon$  .”  **$B \rightarrow 0B \mid 1B \mid \epsilon$** ” does not make this grammar ambiguous.  
 (= unambiguous) The structure of this tree is unique and expands to the right side. Left child must have 0 or 1 and right child must have B or  $\epsilon$  .



Therefore, this grammar is unambiguous. (= produce a unique tree structure)

5.4.5 b) Find a grammar for the same language that is ambiguous, and demonstrate its ambiguity.

$S \rightarrow A1B$

$A \rightarrow 0A \mid A0 \mid \varepsilon$

$B \rightarrow 0B \mid 1B \mid \varepsilon$

For a string  $w=0011$ , two parse trees are produced. Therefore, this grammar is ambiguous.

