

Solutions for Assignment #4

Assignment Information

Maximum grade 20

Due date September 15, 2004

Instructions Textbook
Page 66-67; problems: 2.3.2, 2.3.4
Page 72; problem: 2.4.1 (b) and (c)

2.3.2

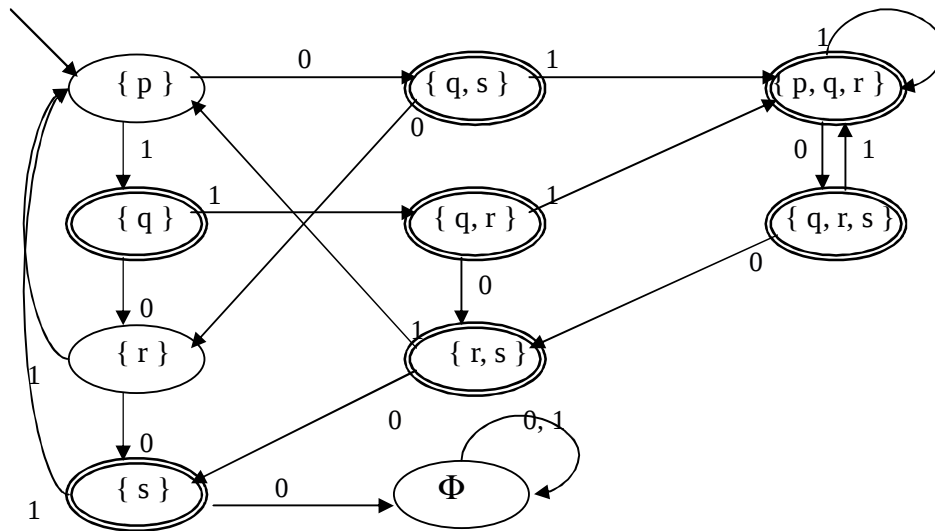
Since given NFA has four states, DFA can have 2^n states. The following is the complete subset construction.

state	0	1
Φ	Φ	Φ
$\rightarrow \{p\}$	$\{q,s\}$	$\{q\}$
$\ast\{q\}$	$\{r\}$	$\{q,r\}$
$\{r\}$	$\{s\}$	$\{p\}$
$\ast\{s\}$	Φ	$\{p\}$
$\ast\{p,q\}$	$\{q,r,s\}$	$\{q,r\}$
$\{p,r\}$	$\{q,s\}$	$\{p,q\}$
$\ast\{p,s\}$	$\{q,s\}$	$\{p,q\}$
$\ast\{q,r\}$	$\{r,s\}$	$\{p,q,r\}$
$\ast\{q,s\}$	$\{r\}$	$\{p,q,r\}$
$\ast\{r,s\}$	$\{s\}$	$\{p\}$
$\ast\{p,q,r\}$	$\{q,r,s\}$	$\{p,q,r\}$
$\ast\{p,q,s\}$	$\{q,r,s\}$	$\{p,q,r\}$
$\ast\{p,r,s\}$	$\{q,s\}$	$\{p,q\}$
$\ast\{q,r,s\}$	$\{r,s\}$	$\{p,q,r\}$
$\ast\{p,q,r,s\}$	$\{q,r,s\}$	$\{p,q,r\}$

We will get the following transition table and diagram after removing the unnecessary states.

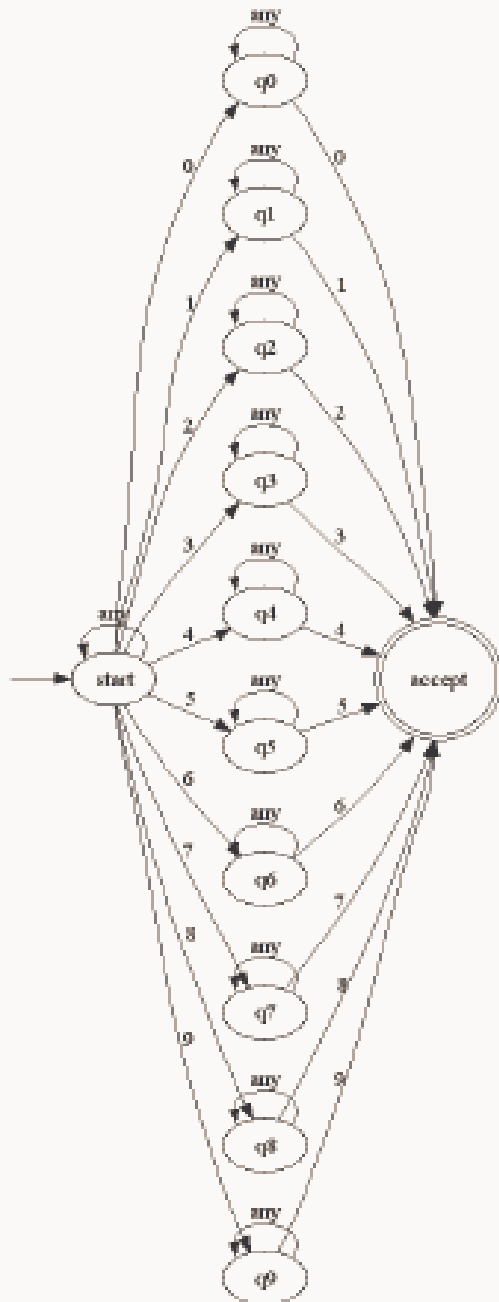
State	0	1
Φ	Φ	Φ
$\rightarrow\{p\}$	$\{q,s\}$	$\{q\}$
$*\{q\}$	$\{r\}$	$\{q,r\}$
$\{r\}$	$\{s\}$	$\{p\}$
$*\{s\}$	Φ	$\{p\}$
$*\{q,s\}$	$\{r\}$	$\{p,q,r\}$
$*\{q,r\}$	$\{r,s\}$	$\{p,q,r\}$
$*\{r,s\}$	$\{s\}$	$\{p\}$
$*\{p,q,r\}$	$\{q,r,s\}$	$\{p,q,r\}$
$*\{q,r,s\}$	$\{r,s\}$	$\{p,q,r\}$

Transition Table



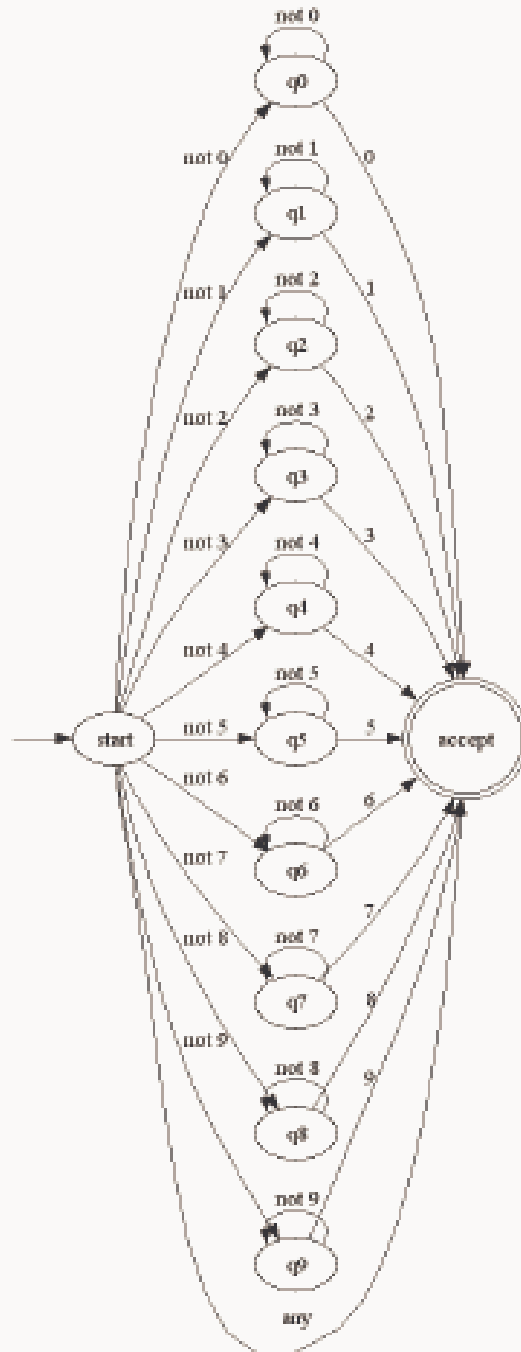
2.3.4

a)



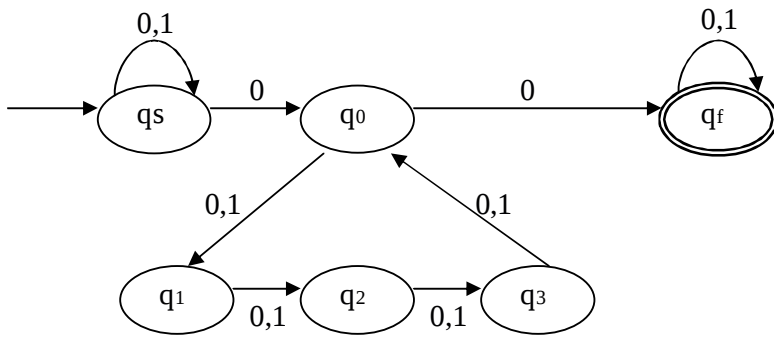
where “any” denotes $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

b)



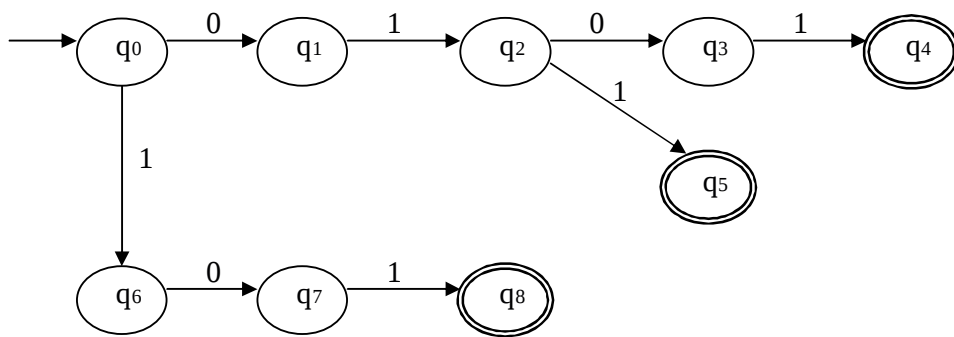
where 'not #' denotes $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\} - \{\#\}$

c)

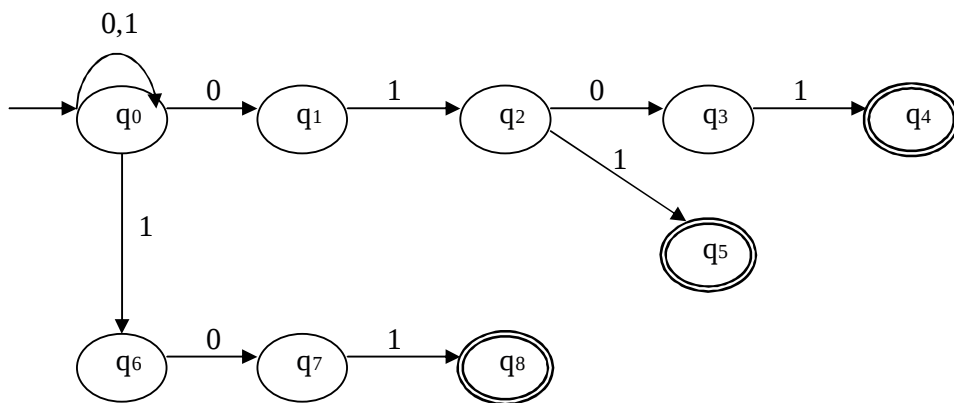


2.4.1

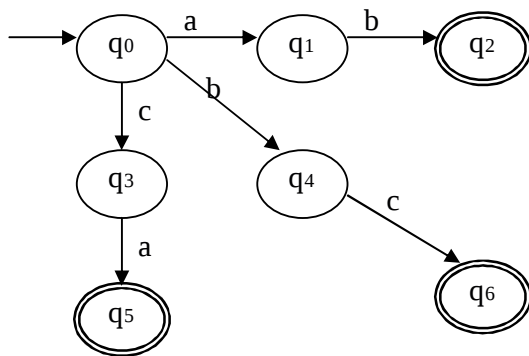
b)



or



c)



or

